

Math Review for Incoming Geometry Honors Students

Solve each equation.

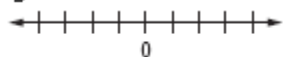
- $5x + 8 = 3 + 2(3x - 4)$
- $-5(2n - 3) = 7(3 - n)$
- Victoria goes to the mall with \$60. She purchases a skirt for \$12 and perfume for \$35.99. She also spends \$3.25 on food. She still wants to buy a belt. How much money can she spend on the belt?
- Nicole makes \$9.50 per hour working at an electronics company. She plans to buy a hand-held computer, the least expensive of which costs \$245.60 and the most expensive of which costs \$368.40. Write and solve an inequality describing how long Nicole will have to work to be able to buy a hand-held computer.

Solve each inequality.

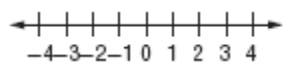
- $3(-w - 6) < 2(2w + 8) + 1$

Solve each compound inequality. Then graph the solution set.

- $\frac{w}{3} < 1$ or $3w + 5 > 11$



- $2 + 3x > 8$ or $4 - 7x \leq -17$



- Write an equation and state the slope for the line that passes through $(9, 22)$ and $(15, 36)$.
- Write the point-slope form, slope-intercept form, and standard form of an equation for a line that passes through $(-1, 2)$ with slope 4.
- Determine whether $y = 4x + 5$ and $y = \frac{1}{4}x - 2$ are perpendicular. Explain.
- Write an equation of the line that is parallel to the graph of $y = -4x + 2$ and passes through $(2, -4)$.
- To fill two new aquariums, Laura bought some saltwater fish for \$2 each and some freshwater fish for \$1 each. If she bought a total of 15 fish and spent a total of \$23, how many fish of each kind did she buy?
- Two trains A and B are 240 miles apart. Both start at the same time and travel toward each other. They meet 3 hours later. The speed of train A is 20 miles faster than train B. Find the speed of each train.
- Scott bought a pen and received change of \$4.75 in 25 coins, all dimes and quarters. How many of each kind did he receive?
- Five times one number added to another number is 32. Three times the first number minus the other number is 8. Find the numbers.
- The graphs of $2x + 3y = 5$ and $3x + y = 18$ contain two of the sides of a triangle. A vertex of the triangle is at the intersection of the graphs. What are the coordinates of the vertex?
- Use the rate formula to write an equation for the distance traveled by a boat upstream against a current and another equation for the distance traveled by a boat downstream with the current, where $r =$ speed of the boat, and $c =$ rate of the current, and $s =$ total speed. Then solve each equation for the time.
- A boat travels 33 miles downstream in 4 hours. The return trip takes the boat 7 hours. Find the speed of the boat in still water.

19. Laura can weed the garden in 1 hour 20 minutes and her husband can weed it in 1 hour 30 minutes. How long will they take to weed the garden together?
20. The inlet pipe of an oil tank can fill the tank in 1 hour 30 minutes. The outlet pipe can empty the tank in 1 hour. How long it will take to empty a full tank if both pipes are open?

Solve the system of inequalities by graphing.

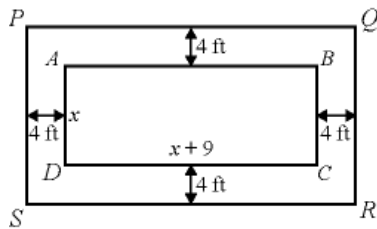
21. $y > x + 2$
 $y \leq -2x - 1$

Determine the best method to solve each system of equations. Then solve the system.

22. $x = 2y - 1$
 $3x + y = 11$

23. $5x - y = 17$
 $3x - y = 13$

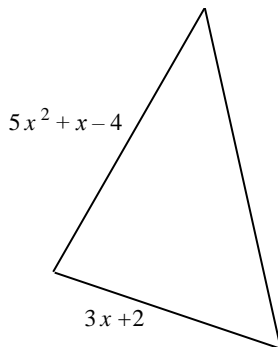
The length of a rectangular garden ABCD is 9 feet more than its width. It is surrounded by a brick walkway 4 feet wide as shown below. Suppose the total area of the walkway is 400 square feet.



24. Write a polynomial to represent the length of PQ .
25. What are the dimensions of the garden?

The measures of two sides of a triangle are given. If P is the perimeter, find the measure of the third side.

26. $P = 8x^2 + 4x - 1$



Simplify. Assume that no denominator is equal to zero.

27. $(3a^2b^5)(-2ab^3)$

28. $4a^4b^8 + 2(ab^2)^4 + 4(a^2b^4)^2$

29. $\frac{4a^{-3}d^2}{8a^2d^{-5}}$

30. $\frac{(3r^3t^5)^3}{(-3r^2t^7)^2}$

Evaluate each product or quotient. Express the results in both scientific notation and standard form.

31. $\frac{1.6 \times 10^3}{8 \times 10^7}$

32. Find the degree of the polynomial $2x^2y - 4x^5 + 6xy^3$.

33. Write $3x^2 - x - 3 + x^3$ in standard form. Identify the leading coefficient.

Find each product.

34. $3x^2y(2x^2y - 5xy^2 + 8y^3x^2)$

35. $(2n + 3)(3n^2 - 4n + 1)$

36. $(5y + 6)^2$

Factor each polynomial, if possible. If the polynomial cannot be factored, write *prime*.

37. $10x^2yz - 22x^3y^2z$

38. $2xy - 4x + 3y - 6$

39. $m^2 + 12m - 28$

40. $5t^2 + 17t - 12$

41. $6p^2 - 20p + 16$

42. $49a^2 - 169$

43. $3x^5 - 75x^3$

44. $81c^2 + 72c + 16$

45. $25x^2 + 70x - 49$

Solve each equation. Check the solutions.

46. $12b^2 - 8b = 0$

47. $y^2 + 4y = 45$

48. $9n^2 + 6n = 3$

Solve each equation by using the Quadratic Formula. Round to the nearest tenth if necessary.

49. $12v^2 - 6 = -v$

50. $d^2 - 14d - 22 = 0$

51. $15n^2 - 3 = 4n$

Simplify each expression.

52. $\sqrt{50x^3y^2}$

53. $\frac{5\sqrt{2}}{\sqrt{10} - 3}$

54. $2\sqrt{24} + \sqrt{54} + 3\sqrt{150}$

55. $(\sqrt{11} - \sqrt{6})(\sqrt{2} + \sqrt{33})$

56. The Distance Formula $d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$ can be used to find the distance between two points (x_1, y_1) and (x_2, y_2) . Find the distance between $(6, 0)$ and $(-5, 4)$.

57. The points $A(-3, b)$, and $B(1, 3)$ are 5 units apart. Find the value of b .

58. Find the area and the perimeter of a square with a side of length $2\sqrt{3} + 6\sqrt{7}$ inches.

59. The length of the base of a right-angled triangle ABC is 6 centimeters and the length of the hypotenuse is 10 centimeters. Find the area of the triangle.

60. Find the coordinates of the midpoint of the segment with endpoints $(7, -1)$ and $(-1, 5)$.

Answers:

Example for 1 – 2.

EXAMPLE 2 Solve an Equation with Grouping Symbols

Solve $6(5m - 3) = \frac{1}{3}(24m + 12)$.

$$6(5m - 3) = \frac{1}{3}(24m + 12) \quad \text{Original equation}$$

$$30m - 18 = 8m + 4 \quad \text{Distributive Property}$$

$$30m - 18 - 8m = 8m + 4 - 8m \quad \text{Subtract } 8m \text{ from each side.}$$

$$22m - 18 = 4 \quad \text{Simplify.}$$

$$22m - 18 + 18 = 4 + 18 \quad \text{Add 18 to each side.}$$

$$22m = 22 \quad \text{Simplify.}$$

$$\frac{22m}{22} = \frac{22}{22} \quad \text{Divide each side by 22.}$$

$$m = 1 \quad \text{Simplify.}$$

- $x = 13$
- $n = -2$
- Victoria can spend no more than \$8.76 on the belt.

$$\$12 + \$35.99 + \$3.25 + x \leq \$60$$

Solve the inequality by subtracting the sum of the constant terms on the left side of the inequality from both sides of the inequality.

- $\$245.60 \leq \$9.50h \leq \$368.40; 25.9 \leq h \leq 38.8$

The product of time worked and money earned per hour must lie between \$245.60 and \$368.40. To solve the inequality, divide each side of the inequality by the coefficient of the variable.

- $\{w | w > -5\}$ Remember – whenever you multiply or divide by a negative, you must flip the inequality symbol.

Example for 6 – 7.

EXAMPLE 3 Solve and Graph a Union

Solve $-2m + 7 \leq 13$ or $5m + 12 > 37$. Then graph the solution set.

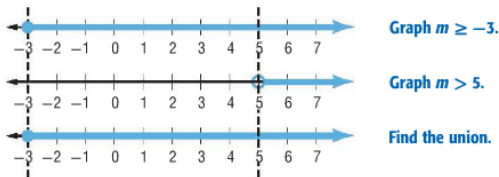
$$-2m + 7 \leq 13 \quad \text{or} \quad 5m + 12 > 37$$

$$-2m + 7 - 7 \leq 13 - 7 \quad \text{Subtract.} \quad 5m + 12 - 12 > 37 - 12$$

$$-2m \leq 6 \quad \text{Simplify.} \quad 5m > 25$$

$$\frac{-2m}{-2} \geq \frac{6}{-2} \quad \text{Divide.} \quad \frac{5m}{5} > \frac{25}{5}$$

$$m \geq -3 \quad \text{Simplify.} \quad m > 5$$

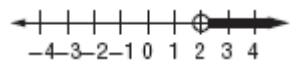


Notice that the graph of $m \geq -3$ contains every point in the graph of $m > 5$. So, the union is the graph of $m \geq -3$. The solution set is $\{m | m \geq -3\}$.

- $\{w | w \text{ is a real number}\}$



- $\{x | x > 2\}$



8. $y = \frac{7}{3}x + 1; \frac{7}{3}$

Find the slope of the line with the slope formula. Find the y -intercept by replacing x and y with the given point and m with the slope in the slope-intercept form. Solve for b . Write the equation in slope-intercept form using the given m and the calculated b .

9. $y - 2 = 4(x + 1); y = 4x + 6; 4x - y = -6$

The linear equation $y - y_1 = m(x - x_1)$ is written in point-slope form, where (x_1, y_1) is a given point on a nonvertical line and m is the slope of the line.

Given an equation in point-slope form, solve the equation for y to find the equation in slope-intercept form.

The linear equation in standard form is given as $Ax + By = C$, where A , B , and C are constants. Use Addition and Subtraction Properties of Equality to rewrite the equation in standard form.

10. No; the slopes are 4 and $\frac{1}{4}$.

Two nonvertical lines are perpendicular if the slopes are opposite reciprocals of each other.

11. $y = -4x + 4$

Two nonvertical lines are parallel if they have the same slope. Use the given point with the slope of the parallel line in the point-slope form. Then change to the slope-intercept form.

12. 8 saltwater fish, 7 freshwater fish

$$x + y = 15$$

$$2x + y = 23$$

Eliminate one variable by subtracting the two equations. Solve for x and then substitute that value into one of the equations to find the value of y .

13. Speed of train A: 50mph, Speed of train B: 30mph

$$x = y + 20$$

$$3x + 3y = 240$$

Substitute $y + 20$ for x in the second equation and solve for y . Substitute that value into the first equation and solve for x .

14. 10 dimes and 15 quarters

$$x + y = 25$$

$$0.10x + 0.25y = 4.75$$

Substitute $25 - x$ for y in the second equation and solve for x . Substitute that value into the first equation and solve for y .

15.5, 7

$$5x + y = 32$$

$$3x - y = 8$$

Eliminate one variable by adding the two equations. Solve for x and then substitute that value into one of the equations to find the value of y .

16. $(7, -3)$

Eliminate the x terms by first multiplying the top equation by 3 and the bottom one by 2 and then subtracting the two equations. Solve for y and then substitute that value into one of the equations to find the value of x .

17. $d = t(r - c), d = t(r + c); t = \frac{d}{r - c}, t = \frac{d}{r + c}$

Use the formula, $d = rt$, to find the equation for the distance traveled by the boat downstream with the current and upstream with the current.

18. 6.48 mph

$$4x + 4y = 33$$

$$7x - 7y = 33$$

Set up problem in same way as number 17. Eliminate the x terms by first multiplying the top equation by 7 and the bottom one by 4 and then subtracting the two equations. Solve for y and then substitute that value into one of the equations to find the value of x .

Example for 19 – 20.

Real-World EXAMPLE 4 Work Problem

JOBS At his part-time job at the zoo, Ping can clean the bird area in 2 hours. Natalie can clean the same area in 1 hour and 15 minutes. How long would it take them if they worked together?

Understand It takes Ping 2 hours to complete the job and Natalie $1\frac{1}{4}$ hours.

You need to find the rate that each person works and the total time t that it will take them if they work together.

Plan Find the fraction of the job that each person can do in an hour.

Ping's rate $\rightarrow \frac{1 \text{ job}}{2 \text{ hours}} = \frac{1}{2}$ job per hour

Natalie's rate $\rightarrow \frac{1 \text{ job}}{1\frac{1}{4} \text{ hours}}$ or $\frac{1 \text{ job}}{\frac{5}{4} \text{ hours}} = \frac{4}{5}$ job per hour

Since rate \cdot time = fraction of job done, multiply each rate by the time t to represent the amount of the job done by each person.

Solve Fraction of job Ping completes plus fraction of job Natalie completes equals 1 job.

$$\frac{1}{2}t + \frac{4}{5}t = 1$$

$$10\left(\frac{1}{2}t + \frac{4}{5}t\right) = 10(1) \quad \text{Multiply each side by the LCD, 10.}$$

$$10\left(\frac{1}{2}t\right) + 10\left(\frac{4}{5}t\right) = 10 \quad \text{Distributive Property}$$

$$5t + 8t = 10 \quad \text{Simplify.}$$

$$t = \frac{10}{13} \quad \text{Add like terms and divide each side by 13.}$$

So, it would take them $\frac{10}{13}$ hour or about 46 minutes to complete the job if they work together.

Check In $\frac{10}{13}$ hour, Ping would complete $\frac{1}{2} \cdot \frac{10}{13}$ or $\frac{5}{13}$ of the job and Natalie would complete $\frac{4}{5} \cdot \frac{10}{13}$ or $\frac{8}{13}$ of the job. Together, they complete $\frac{5}{13} + \frac{8}{13}$ or 1 whole job. So, the answer is reasonable. ✓

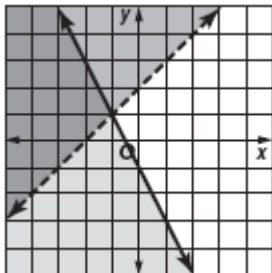
19. about 42.4 minutes

Time taken to weed the garden if Laura and her husband worked together is $\frac{1}{1\frac{1}{3}} + \frac{1}{1\frac{1}{2}}$ h.

20. 3 h

Time taken to empty a full tank if both pipes are open is $1 - \frac{1}{1\frac{1}{2}}$ h.

21.



22. substitution; (3, 2)

23. elimination with subtraction; (2, -7)

24. $x + 17$

Length of PQ is the sum of the length of the garden and the width of the walkway.

25. 16.5 ft by 25.5 ft

The total area of the walkway is 400 square feet, which is the difference between the area of garden along with walkway and the area of garden. Solve for x to find the dimensions of the garden.

26. $3x^2 + 1$

The perimeter of a triangle is the sum of the three sides. Group like terms together. Subtract like terms, making sure you subtract negatives (add). The power stays the same.

Rules for exponents:

For any nonzero real numbers a and b and any integers m , n , and p , the following are true.

Multiplying Monomials (Lesson 7-1)

- Product of Powers: $a^m \cdot a^n = a^{m+n}$
- Power of a Power: $(a^m)^n = a^{m \cdot n}$
- Power of a Product: $(ab)^m = a^m b^m$

Dividing Monomials (Lesson 7-2)

- Quotient of Powers: $\frac{a^m}{a^p} = a^{m-p}$
- Power of a Quotient: $\left(\frac{a}{b}\right)^m = \frac{a^m}{b^m}$
- Zero Exponent: $a^0 = 1$
- Negative Exponent: $a^{-n} = \frac{1}{a^n}$ and $\frac{1}{a^{-n}} = a^n$

27. $-6a^3b^8$

28. $10a^4b^8$

29. $\frac{d^7}{2b^5}$

30. $3r^5t$

Example for 31.

EXAMPLE 4 Divide with Scientific Notation

Evaluate $\frac{3.066 \times 10^8}{7.3 \times 10^3}$. Express the result in both scientific notation and standard form.

$$\begin{aligned}\frac{3.066 \times 10^8}{7.3 \times 10^3} &= \left(\frac{3.066}{7.3}\right) \left(\frac{10^8}{10^3}\right) && \text{Product rule for fractions} \\ &= 0.42 \times 10^5 && \text{Quotient of Powers} \\ &= 4.2 \times 10^{-1} \times 10^5 && 0.42 = 4.2 \times 10^{-1} \\ &= 4.2 \times 10^4 && \text{Product of Powers} \\ &= 42,000 && \text{Standard form}\end{aligned}$$

31. 2×10^{-3} ; .002

Example for 32 – 33.



EXAMPLE 3 Standard Form of a Polynomial

Write each polynomial in standard form. Identify the leading coefficient.

a. $3x^2 + 4x^5 - 7x$

Step 1 Find the degree of each term.

Degree: $\begin{matrix} 2 & 5 & 1 \\ \uparrow & \uparrow & \uparrow \end{matrix}$
Polynomial: $3x^2 + 4x^5 - 7x$

Step 2 Write the terms in descending order: $4x^5 + 3x^2 - 7x$.

The leading coefficient is 4.

b. $5y - 9 - 2y^4 - 6y^3$

Step 1 Degree: $\begin{matrix} 1 & 0 & 4 & 3 \\ \uparrow & \uparrow & \uparrow & \uparrow \end{matrix}$
Polynomial: $5y - 9 - 2y^4 - 6y^3$

Step 2 $-2y^4 - 6y^3 + 5y - 9$ The leading coefficient is -2 .

32. 5

33. $x^3 + 3x^2 - x - 3$; 1

34. $6x^4y^2 - 15x^3y^3 + 24x^4y^4$

35. $6n^3 + n^2 - 10n + 3$

36. $25y^2 + 60y + 36$

Examples for 37 – 48.

EXAMPLE 3

Factor $12y^2 + 9y + 8y + 6$.

$$12y^2 + 9y + 8y + 6$$

$$= (12y^2 + 9y) + (8y + 6)$$

Group terms with common factors.

$$= 3y(4y + 3) + 2(4y + 3)$$

Factor the GCF from each group.

$$= (4y + 3)(3y + 2)$$

Distributive Property

EXAMPLE 4

Solve $x^2 - 6x = 0$. Check your solutions.

Write the equation so that it is of the form $ab = 0$.

$$x^2 - 6x = 0$$

Original equation

$$x(x - 6) = 0$$

Factor by using the GCF.

$$x = 0 \quad \text{or} \quad x - 6 = 0$$

Zero Product Property

$$x = 6$$

Solve.

The roots are 0 and 6. Check by substituting 0 and 6 for x in the original equation.

EXAMPLE 5

Factor $x^2 + 10x + 21$

$b = 10$ and $c = 21$, so $m + p$ is positive and mp is positive. Therefore, m and p must both be positive. List the positive factors of 21, and look for the pair of factors with a sum of 10.

Factors of 21	Sum of 10
1, 21	22
3, 7	10

The correct factors are 3 and 7.

$$\begin{aligned} x^2 + 10x + 21 &= (x + m)(x + p) && \text{Write the pattern.} \\ &= (x + 3)(x + 7) && m = 3 \text{ and } p = 7 \end{aligned}$$

EXAMPLE 6

Factor $12a^2 + 17a + 6$

$a = 12$, $b = 17$, and $c = 6$. Since b is positive, $m + p$ is positive. Since c is positive, mp is positive. So, m and p are both positive. List the factors of $12(6)$ or 72, where both factors are positive.

Factors of 72	Sum of 17
1, 72	73
2, 36	38
3, 24	27
4, 18	22
6, 12	18
8, 9	17

The correct factors are 8 and 9.

$$\begin{aligned} 12a^2 + 17a + 6 &= 12a^2 + ma + pa + 6 \\ &= 12a^2 + 8a + 9a + 6 \\ &= (12a^2 + 8a) + (9a + 6) \\ &= 4a(3a + 2) + 3(3a + 2) \\ &= (3a + 2)(4a + 3) \end{aligned}$$

$$\text{So, } 12a^2 + 17a + 6 = (3a + 2)(4a + 3).$$

EXAMPLE 7

Solve $x^2 - 4 = 12$ by factoring.

$$x^2 - 4 = 12$$

Original equation

$$x^2 - 16 = 0$$

Subtract 12 from each side.

$$x^2 - (4)^2 = 0$$

$$16 = 4^2$$

$$(x + 4)(x - 4) = 0$$

Factor the difference of squares.

$$x + 4 = 0 \quad \text{or} \quad x - 4 = 0$$

Zero Product Property

$$x = -4$$

$$x = 4$$

Solve each equation.

The solutions are -4 and 4 .

37. $2x^2yz(5 - 11xy)$

38. $(y - 2)(2x + 3)$

39. $(m + 14)(m - 2)$

40. $(5t - 3)(t + 4)$

41. $2(3p - 4)(p - 2)$

42. $(7a + 13)(7a - 13)$

43. $3x^2(x + 5)(x - 5)$

44. $(9c + 4)^2$

45. prime

46. $\left[0, \frac{2}{3}\right]$

47. $\{-9, 5\}$

48. $\left[-1, \frac{1}{3}\right]$

Examples for 49 – 51.

EXAMPLE 2 Use the Quadratic Formula

Solve each equation by using the Quadratic Formula. Round to the nearest tenth if necessary.

a. $3x^2 + 5x - 12 = 0$

For this equation, $a = 3$, $b = 5$, and $c = -12$.

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a} \quad \text{Quadratic Formula}$$

$$= \frac{-(5) \pm \sqrt{(5)^2 - 4(3)(-12)}}{2(3)} \quad a = 3, b = 5, \text{ and } c = -12$$

$$= \frac{-5 \pm \sqrt{25 + 144}}{6} \quad \text{Multiply.}$$

$$= \frac{-5 \pm \sqrt{169}}{6} \text{ or } \frac{-5 \pm 13}{6} \quad \text{Add and simplify.}$$

$$x = \frac{-5 - 13}{6} \text{ or } x = \frac{-5 + 13}{6} \quad \text{Separate the solutions.}$$

$$= -3 \quad = \frac{4}{3} \quad \text{Simplify.}$$

The solutions are -3 and $\frac{4}{3}$.

b. $10x^2 - 5x = 25$

Step 1 Rewrite the equation in standard form.

$$10x^2 - 5x = 25 \quad \text{Original equation}$$

$$10x^2 - 5x - 25 = 0 \quad \text{Subtract 25 from each side.}$$

Step 2 Apply the Quadratic Formula.

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a} \quad \text{Quadratic Formula}$$

$$= \frac{-(-5) \pm \sqrt{(-5)^2 - 4(10)(-25)}}{2(10)} \quad a = 10, b = -5, \text{ and } c = -25$$

$$= \frac{5 \pm \sqrt{25 + 1000}}{20} \quad \text{Multiply.}$$

$$= \frac{5 \pm \sqrt{1025}}{20} \quad \text{Add.}$$

$$= \frac{5 - \sqrt{1025}}{20} \text{ or } \frac{5 + \sqrt{1025}}{20} \quad \text{Separate the solutions.}$$

$$\approx -1.4 \quad \approx 1.9 \quad \text{Simplify.}$$

The solutions are about -1.4 and 1.9 .

49. $-\frac{3}{4}, \frac{2}{3}$

50. $1.8, 12.2$

51. $-\frac{1}{3}, \frac{3}{5}$

Examples for 52 – 55.

EXAMPLE 3 Simplify a Square Root with Variables

Simplify $\sqrt{90x^3y^4z^5}$.

$$\begin{aligned}\sqrt{90x^3y^4z^5} &= \sqrt{2 \cdot 3^2 \cdot 5 \cdot x^3 \cdot y^4 \cdot z^5} \\ &= \sqrt{2} \cdot \sqrt{3^2} \cdot \sqrt{5} \cdot \sqrt{x^2} \cdot \sqrt{x} \cdot \sqrt{y^4} \cdot \sqrt{z^4} \cdot \sqrt{z} \\ &= \sqrt{2} \cdot 3 \cdot \sqrt{5} \cdot |x| \cdot \sqrt{x} \cdot y^2 \cdot z^2 \cdot \sqrt{z} \\ &= 3y^2z^2x\sqrt{10xz}\end{aligned}$$

Prime factorization

Product Property

Simplify.

Simplify.

EXAMPLE 2

Simplify $\frac{2}{4 + \sqrt{3}}$.

$$\begin{aligned}\frac{2}{4 + \sqrt{3}} &= \frac{2}{4 + \sqrt{3}} \cdot \frac{4 - \sqrt{3}}{4 - \sqrt{3}} \\ &= \frac{2(4) - 2\sqrt{3}}{4^2 - (\sqrt{3})^2} \\ &= \frac{8 - 2\sqrt{3}}{16 - 3} \\ &= \frac{8 - 2\sqrt{3}}{13}\end{aligned}$$

Rationalize the denominator.

$$(a - b)(a + b) = a^2 - b^2$$

$$(\sqrt{3})^2 = 3$$

Simplify.

EXAMPLE 4

Simplify $(\sqrt{3} - \sqrt{2})(\sqrt{3} + 2\sqrt{2})$.

$$\begin{aligned}(\sqrt{3} - \sqrt{2})(\sqrt{3} + 2\sqrt{2}) &= (\sqrt{3})(\sqrt{3}) + (\sqrt{3})(2\sqrt{2}) + (-\sqrt{2})(\sqrt{3}) + (\sqrt{2})(2\sqrt{2}) \\ &= 3 + 2\sqrt{6} - \sqrt{6} + 4 \\ &= 7 + \sqrt{6}\end{aligned}$$

52. $5|xy|\sqrt{2x}$
 53. $10\sqrt{5} + 15\sqrt{2}$
 54. $2\sqrt{y}$
 55. $22\sqrt{6}$
 56. $\sqrt{137}$

Substitute the given values in the Distance Formula. Use the Product Property of square roots. Then simplify the result.

57. $b = 0$ or 6

Substitute the given values in the Distance Formula. Evaluate the squares. Solve for the missing variable.

58. $264 + 24\sqrt{21} \text{ in.}^2, 8\sqrt{3} + 24\sqrt{7} \text{ in.}$

The area of a square is s^2 , where s is the side of the square and the formula for the perimeter of a rectangle is $4s$, where s is the side of the square. Replace the variables in the formula with the given values. Use the Product Property of square roots. Then simplify the result.

59. 24 cm^2

Find the height of the triangle by the Pythagorean theorem ($a^2 + b^2 = c^2$). The area of a triangle is $\frac{1}{2} \times \text{base} \times \text{height}$. Replace the variables in the formula and solve.

60. $(3, 2)$